

# Package ‘polyMatrix’

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**Version** 0.3.1

**Title** Infrastructure for Manipulation Polynomial Matrices

**Description**

Implementation of class ``polyMatrix" for storing a matrix of polynomials and implements basic matrix operations; including a determinant and characteristic polynomial. It is based on the package 'polynom' and uses a lot of its methods to implement matrix operations. This package includes 3 methods of triangularization of polynomial matrices: Extended Euclidean algorithm which is most classical but numerically unstable; Sylvester algorithm based on LQ decomposition; Interpolation algorithm is based on LQ decomposition and Newton interpolation. Both methods are described in D. Henrion & M. Sebek, Reliable numerical methods for polynomial matrix triangularization, IEEE Transactions on Automatic Control (Volume 44, Issue 3, Mar 1999, Pages 497-508) <doi:10.1109/9.751344> and in Salah Labhalla, Henri Lombardi & Roger Marlin, Algorithmes de calcul de la reduction de Hermite d'une matrice a coefficients polynomeaux, Theoretical Computer Science (Volume 161, Issue 1-2, July 1996, Pages 69-92) <doi:10.1016/0304-3975(95)00090-9>.

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**License** MIT + file LICENSE

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polyMatrix-package      *Infrastructure for Manipulation Polynomial Matrices*

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**Description**

Implementation of class "polyMatrix" for storing a matrix of polynomials and implements basic matrix operations; including a determinant and characteristic polynomial. It is based on the package 'polynom' and uses a lot of its methods to implement matrix operations. This package includes 3 methods of triangularization of polynomial matrices: Extended Euclidean algorithm which is most classical but numerically unstable; Sylvester algorithm based on LQ decomposition; Interpolation algorithm is based on LQ decomposition and Newton interpolation. Both methods are described in D. Henrion & M. Sebek, Reliable numerical methods for polynomial matrix triangularization, IEEE Transactions on Automatic Control (Volume 44, Issue 3, Mar 1999, Pages 497-508) <doi:10.1109/9.751344> and in Salah Labhalla, Henri Lombardi & Roger Marlin, Algorithmes de calcul de la reduction de Hermite d'une matrice a coefficients polynomeaux, Theoretical Computer Science (Volume 161, Issue 1-2, July 1996, Pages 69-92) <doi:10.1016/0304-3975(95)00090-9>.

**Details**

Package: polyMatrix  
Type: Package  
Version: 0.0.05  
Date: 2016-06-04  
License: GPL-3

Infrastructure for manipulation polynomial matrices.

**Author(s)**

NA  
Maintainer: NA

**References**

See other polynomial packages: polynom, PolynomF, MonoPoly, multipol, mpol, orthopolynom.

**Examples**

```
# the c("polyMarray", "polyMatrix") class structure
str(polyMgen.a())

# the c("polyMbroad", "polyMatrix") class structure
str(polyMgen.b())

# the c("polyMcells", "polyMatrix") class structure
str(polyMgen.c())

# the c("polyMdlist", "polyMatrix") class structure
str(polyMgen.d())
```

---

CanForm

*Conversion of an ARMA representation to a canonical form*


---

**Description**

The representation of an ARMA processes is unambiguous only in canonical form. The CanForm method, if the necessary parameters are given converts the ARMA representation to echelon, final or scm form.

**Usage**

```
CanForm(pM, form)
CanForm.echelon(pM)
CanForm.final(pM)
CanForm.scm(pM)
```

**Arguments**

pM                    an arbitrary pMvarma class object  
form                    an arbitrary or "echelon", "final", "scm" form code

**Value**

An pMvarma class object in echelon, final or scm form.

**Note**

This method doesn't work yet - is not implemented yet.

**See Also**

[polyMatrix-package](#)

## Examples

```
parma <- polyMgen.varma(3,3,rand=TRUE,degree=c(1,1))
parma

CanForm(parma,"final")
CanForm(parma,"echelon")
CanForm(parma,"scm")

# clean up
# rm(parma)
```

---

ch2pn

*Converts a character class object to a polynomial class object*

---

## Description

Receives a character class object – which looks like the print image of a polynomial object – and returns a polynomial class object.

## Usage

```
ch2pn(chv, symb = "x")
```

## Arguments

chv            a character class object like the print image of a polynomial object  
symb           the required symbol of input polynom string

## Details

This technical subrutin converts a character object to a polynomial object. The "x" is the default symbol in the input string. The output is a polynomial or a list of polynomials, without any defined symbol. The default `print.polynomial` writes out the output by the symbol "x".

## Value

A polynomial class object or a list of polynomial objects.

## See Also

[pn2ch](#), [pprt](#)

**Examples**

```

chx <- "1 + x + x^3 + 2 * x^4 - 4 * x^5 - 15 * x^16"
p <- ch2pn(chx, "x")
# "polynomial" (as in package: 'polynom')
class(p)
# 1 + x + x^3 + 2*x^4 - 4*x^5 - 15*x^16
p
# ditto <= 'x' is the default symbol
ch2pn(chx)

# the same polynom over 'z'
chz <- "1 + z + z^3 + 2 * z^4 - 4 * z^5 - 15 * z^16"
# == 1: the only "x" power in the input string
ch2pn(chz)
# 1 + x + x^3 + 2*x^4 - 4*x^5 - 15*x^16
ch2pn(chz, "z")

# the same print by polyMatrix::pprt() print utility
pprt(ch2pn(chz, "z"), "x")

# 1 + 5*x - 5*x^2 - 2*x^3 + x^5 + x^6 - x^7
ch2pn("-2 * x^3 - 5 * x^2 + x^5 + x^6 + 5 * x - x^7 + 1")
# 1
ch2pn("-2 * x^3 - 5 * x^2 + x^5 + x^6 + 5 * x - x^7 + 1", "z")

# 2
ch2pn(" 2")
# 0
ch2pn("z^3")
# z^4
ch2pn("z^3", "z")

# 0
ch2pn(" 3 * z ^ 2 + 5 * z^3")
# 4
ch2pn(" 4 + 5 * z^3")
# 6 + 5*x^3
ch2pn(" 6 + 5 * z^3", "z")

# a list of 'polynomial' class elements: [[1]] x [[2]] 1 + x^2
ch2pn(c(" x ", " 1 + x^2 "))

# col.wise a "polyMdlist" "polyMatrix" class object
polyMgen.d(2, 2, rawData=ch2pn(c("1", "x^2", "x", "0")))

# symbole given for output
polyMgen.d(2, 2, rawData=ch2pn(c("1", "x^2", "x", "0")), symb="x")

# symbole given for input and output
polyMgen.d(2, 2, rawData=ch2pn(c("1", "x^2", "x", "0"), symb="x"), symb="x")

```

```
# clean up
# rm(chz, p, chx)
```

---

charpn	<i>The characteristic polynomial of a matrix or a polynomial matrix</i>
--------	-------------------------------------------------------------------------

---

### Description

The characteristic polynomial of a polynomial matrix is a polynomial with polynomial coefficients.

### Usage

```
charpn(M)
```

### Arguments

**M** polynomial matrix object of `polyMatrix` class

### Value

`det(sI-M)`. When the input is a matrix class object then the value is a polynomial object. When the input is a `polyMatrix` class object then a value is `charpn` class object, which is a list of polynomial objects.

### Note

The solution of the algorithm is simple one, a signed sum of products. There are more elegant and efficient solutions.

### See Also

[predict.charpn](#)

### Examples

```
M1<-matrix(c(2,1,-1,0),2,2,byrow=TRUE)
class(M1) # "matrix"
pM1<-M2pM(M1,"polyMdlst") # conversion matrix => polyMatrix
class(pM1) # "polyMdlst" "polyMatrix"

M2<-matrix(c(1,0,-1,2,1,-1,0,1,1),3,3,byrow=TRUE)
class(M2) # "matrix"
pM2<-M2pM(M2,"polyMdlst") # conversion matrix => polyMatrix
class(pM2) # "polyMdlst" "polyMatrix"

pM3<-polyMgen.d(2,2,rawData=ch2pn(c("1","x^2","x","0")))
class(pM3) # "polyMdlst" "polyMatrix"

pM4<-polyMgen.d(2,2,rawData=ch2pn(c("x","1","x^2","0")))
class(pM4) # "polyMdlst" "polyMatrix"
```

```

class(pM4) # "polyMdlst" "polyMatrix"

pM5<-polyMgen.d(3,3,rawData=ch2pn(c("x","1","x^2","0","x","1","x^2","0","x^2")))
class(pM5) # "polyMdlst" "polyMatrix"

pM6<-polyMgen.d(3,3,rawData=ch2pn(c("x","1","x^2","0","x^2","0","x^2","0","x^2")))
class(pM6) # "polyMdlst" "polyMatrix"

ls() # M1, pM1, M2, pM2, pM3, pM4, pM5, pM6

# ~~~~~
# the eigenvalues of a matrix are
# roots of the characteristic polynomial

pn1 <- charpn(M1) # the characteristic polynom of M1
ev <- eigen(M1)$values
ev # 1 1
predict(pn1,ev) # OK: zero matrix

pn2 <- charpn(M2) # the characteristic polynom of M2
ev <- eigen(M2)$values
round(ev,3) # 1.5+1.323i 1.5-1.323i 0.0+0.000i
round(predict(pn2,ev)) # OK: 0+0i 0+0i 0+0i

# clean up
# rm(pn1, pn2, ev)

# ~~~~~
# the characteristic polynomial and
# the Cayley-Hamilton theorem for 'matrix' and 'polyMatrix' class objects

# ---
# M1, pM1: a 2x2 constant matrix

class(M1) # "matrix"
pn1 <- charpn(M1) # the characteristic polynom of M1
predict(pn1,M1) # OK: zero matrix

class(pM1) # "polyMdlst" "polyMatrix"
pn1p <- charpn(pM1) # the characteristic polynom of pM1
predict(pn1p,pM1) # OK: zero matrix

# ---
# M2, pM2: a 3x3 constant matrix

class(M2) # "matrix"
pn2 <- charpn(M2) # the characteristic polynom of M2
predict(pn2,M2) # OK: zero matrix

class(pM2) # "polyMdlst" "polyMatrix"
pn2p<-charpn(pM2) # the characteristic polynom of pM2
predict(pn2p,pM2) # OK: zero matrix

```



```

# ---
# pM3, pM4: an arbitrary 2x2 polyMatrix

class(pM3) # "polyMdlst" "polyMatrix"
pn3p<-charpn(pM3) # the characteristic polynom of pM3
predict(pn3p,pM3) # OK: zero matrix

class(pM4) # "polyMdlst" "polyMatrix"
pn4p<-charpn(pM4) # the characteristic polynom of pM4
predict(pn4p,pM4) # OK: zero matrix

# ---
# pM5, pM6: an arbitrary 3x3 polyMatrix

class(pM5) # "polyMdlst" "polyMatrix"
pn5p<-charpn(pM5) # the characteristic polynom of pM4
predict(pn5p,pM5) # OK: zero matrix

class(pM6) # "polyMdlst" "polyMatrix"
pn6p<-charpn(pM6) # the characteristic polynom of pM4
predict(pn6p,pM6) # OK: zero matrix

# ~~~~~
ls()

#      1.    2. | 3.    4. | 5.    6. | 7.    8.
# case  real const.pn| real const.pn| arb.pn arb.pn| arb.pn arb.pn
# size  2x2  2x2 | 3x3  3x3 | 2x2  2x2 | 3x3  3x3
# matrices: M1  pM1 | M2   pM2 | pM3  pM4 | pM5  pM6
# char.pn: pn1  pn1p | pn2  pn2p | pn3p  pn4p | pn5p  pn6p

# ~~~~~

# clean up
# rm(M1, M2, pM1, pM2, pM3, pM4, pM5, pM6)
# rm(pn1, pn1p, pn2, pn2p, pn3p, pn4p, pn5p, pn6p)

```

---

coefs

*The coefficients of a polynom or polynomial matrix*


---

### Description

Returns the coefficients of the given polynom or polynomial matrix.

### Usage

```
coefs(p, degree="all")
```

**Arguments**

p                    a polynomial or polyMatrix class object  
 degree             "all" or the serial number of the requested coefficients.

**Details**

The `coefs` consists of two methods. One for a polynomial objects, the other one for polyMatrix objects.

**Value**

A vector of the requested coefficients of the input polynom or a list of the requested coefficient matrices of the input polyMatrix.

**See Also**

[const](#), [lead](#), [coefs.polynomial](#), [coefs.polyMatrix](#)

**Examples**

```
coefs(polynom::polynomial(12:0))
coefs(polynom::polynomial(12:0),degree=c(2,3))
coefs(polyMgen.a())
coefs(polyMgen.b())
coefs(polyMgen.c())
coefs(polyMgen.d())
coefs(polyMgen.d(),degree=1)
```

---

CommonPolynom

*GCD and LCM for polynomial matrices*

---

**Description**

The greatest common divisor of polynomial that keeps the elements of the given polynomial matrix.

**Usage**

```
## S3 method for class 'polyMatrix'
GCD(x, type=OPERATION_TYPE_TOTAL, ...)
## S3 method for class 'polyMatrix'
LCM(x, type=OPERATION_TYPE_TOTAL, ...)
```

**Arguments**

x                    an polyMatrix class object  
 type                calculates the common polynom column-wise (type="col"), row-wise (type="row")  
                      or for the total matrix (type="total", by-default)  
 ...                 additional arguments

**Details**

Calculates the greatest common divisor or the least common divisor of the total matrix, or row-wise or column-wise, depending on the parameter type.

Possible operator types: OPERATION\_TYPE\_TOTAL="total", OPERATION\_TYPE\_COLUMN="col", OPERATION\_TYPE\_ROW="row"

**Value**

A polynomial matrix which is the greatest common divisor or the least common multiple for all the elements of the given polynomial matrix or for the columns or for the rows, depending on the value of the 'type' parameter.

**See Also**

[pMdet](#), [pMadj](#)

**Examples**

```
p1 <- ch2pn("1 - x")
p2 <- ch2pn("x - x^2")
p3 <- ch2pn("1 - x^2")
p4 <- ch2pn("1 + x")
p5 <- ch2pn("1 + 2*x + x^2")
p6 <- ch2pn("1 - 2*x + x^2")
A <- polyMgen.d(2, 3, rawData=list(p1, p2, p3, p4, p5, p6))
A
# 1 - x      1 - x^2    1 + 2*x + x^2
# x - x^2    1 + x      1 - 2*x + x^2

l<-function(...) structure(list(...), class = "polylist")

GCD(A) # 1
polynom::GCD(l(p1, p2, p3, p4, p5, p6)) # 1

GCD(A, "col") # 1
list(
  polynom::GCD(l(p1, p2)),
  polynom::GCD(l(p3, p4)),
  polynom::LCM(l(p5, p6))
)
# 1 - x; 1 + x; 1 - 2*x^2 + x^4

polynom::GCD(l(p1, p2))
polynom::GCD(l(p3, p4))
polynom::LCM(l(p5, p6))

GCD(A, "row") # 1; 1
polynom::GCD(l(p1, p3, p5))
polynom::GCD(l(p2, p4, p6)) # 1; 1

# ---
```

```

LCM(A)
polynom::LCM(l(p1, p2, p3, p4, p5, p6))
# 0.25*x - 0.5*x^3 + 0.25*x^5

LCM(A, "col") # x - x^3
list(
  polynom::LCM(l(p1, p2)),
  polynom::LCM(l(p3, p4)),
  polynom::LCM(l(p5, p6))
)
# x - x^2; 1 - x^2; 1 - 2*x^2 + x^4

LCM(A, "row") # x - x^3
list(
  polynom::LCM(l(p1, p3, p5)),
  polynom::LCM(l(p2, p4, p6))
)
# 0.5 + 0.5*x - 0.5*x^2 - 0.5*x^3; 0.5*x - 0.5*x^2 - 0.5*x^3 + 0.5*x^4

# clean up
# rm(A, p1, p2, p3, p4, p5, p6, l)

```

---

const

*The constant of a polynomial or a polynomial matrix*


---

### Description

Returns the constant of a `polynom` class object or the constant matrix of a `polyMatrix` class object.

### Usage

```
const(p)
```

### Arguments

`p` a `polynomial` or `polyMatrix` class object

### Value

A numeric object, containing the constant of the given polynomial, or of a matrix class object which contains the constant matrix of the given polynomial matrix.

### See Also

[coefs](#), [lead](#), [const.polyMatrix](#), [const.polynomial](#)

**Examples**

```

const(polynom::polynomial(0:12))
const(polyMgen.a())
const(polyMgen.b())
const(polyMgen.c())
const(polyMgen.d())

```

---

constConv

*Conversion of constant matrices*


---

**Description**

Conversion between the 'matrix' and 'polyMatrix' class representation of constant matrices.

**Usage**

```

M2pM(m, class=CLASS_MARRAY)
pM2M(pM)

```

**Arguments**

m	a matrix class object
class	the required class of the value: CLASS_MARRAY, CLASS_MBROAD, CLASS_MCELLS, and CLASS_MDLIST
pM	a polyMatrix class object

**Details**

M2pM converts the matrix class objects to an polyMatrix class object. pM2M converts the zero degree polyMatrix class objects to an matrix object.

**Value**

The M2pM(m) returns the given 'm' matrix in 'polyMatrix' class form. The pM2M(pM) returns the given 'pM' polynomial matrix in 'matrix' class form, if it is a constant matrix, otherwise gives an error message.

**See Also**

[coefs](#), [lead](#), [degree](#)

### Examples

```
m <- matrix(1:12, 3,4)
m
pM <- M2pM(m)
class(pM)
pM

M2pM(m, "polyMarray")
M2pM(m, "polyMbroad")
M2pM(m, "polyMcells")
M2pM(m, "polyMdlist")

# clean up
# rm(m, pM)
```

---

cycFill	<i>A vector or a list of a given length, filled cyclically by the given material</i>
---------	--------------------------------------------------------------------------------------

---

### Description

Fills an object by the given material

### Usage

```
cycFill(data, size)
```

### Arguments

data	the material
size	the desired length

### Details

The class of the output is the same as the class of the input. The output object is filled cyclically by the given material u.

### Value

Depending on the class of the given material, the class of the result is vector or list. The length of the result equals by the value of the size parameter.

### See Also

Used in the code of [polyMgen.a](#),  
[polyMgen.d](#)

**Examples**

```
u <- c(4, 1, 3, 2)
cycFill(u, 2)
cycFill(u, 4)
cycFill(u, 6)
cycFill(u, 11)
cycFill(u, 12)

u <- as.list(c(4, 1, 3, 2))
cycFill(u, 2)
cycFill(u, 4)
cycFill(u, 6)
cycFill(u, 11)
cycFill(u, 12)

# clean up
# rm(u)
```

---

degree

*The degree of a polynomial or a polynomial matrix*

---

**Description**

The degree of the highest non-zero coefficient of the polynomials.

**Usage**

```
degree(p, ...)
```

**Arguments**

`p` a `polynomial` or `polyMatrix` class object  
`...` supplementary options (see `degree.polyMatrix`)

**Value**

When the input is a `polynomial` class object, then value is the degree of the polynomial.

When the input is a `polyMatrix` class object, then in case of `method="matrix"` the value is a matrix by the same size as the input, containing the degrees of the polynomials. In case of `method="column"` or `method="row"` the value are maximums of the columns or rows of the polynomial matrix degrees. In case of `method="default"` it is the maximum of the degree of all polynomials.

**See Also**

[lead](#), [degree.polyMatrix](#), [degree.polynomial](#)

**Examples**

```

p <- polynom::polynomial(0:12)
class(p) # polynom
degree(p)

pM <- polyMgen.d(3,3,rawData=
  ch2pn(c("-3+x^3", "2+4*x", "x^2", "1", "2", "3+x", "2*x", "0", "2-3*x")))
pM

degree(pM) # the maximum degree
degree(pM,"c") # column wise maximum degree
degree(pM,"r") # row wise maximum degree
degree(pM,"m") # matrix: element wise degree

degree(polyMconvert(pM,"polyMarray"),"m") # polyMarray class
degree(polyMconvert(pM,"polyMbrod"),"m") # polyMbrod class
degree(polyMconvert(pM,"polyMcells"),"m") # polyMcells class
degree(polyMconvert(pM,"polyMdlist"),"m") # polyMdlist class

# clean up
# rm(p, pM)

```

---

diag	<i>Extracts the diagonal of a polyMatrix, or constructs a diagonal polyMatrix</i>
------	-----------------------------------------------------------------------------------

---

**Description**

If the input is a polyMatrix then the output is its diagonal. If the input is a vector then the output is a diagonal matrix.

**Usage**

```
diag(x, nrow=NULL, ncol=NULL, names=NULL, type=CLASS_LIST, ...)
```

**Arguments**

x	input material for the diagonal matrix
nrow	number of rows in the output object
ncol	number of columns in the output object
names	(when 'x' is a matrix) logical indicating if the resulting vector, the diagonal of 'x', should inherit 'names' from 'dimnames(x)' if available.
type	the required form and class of the result: CLASS_LIST or CLASS_MATRIX
...	...



## Details

The `diag` has two different applications. When the class of the first input parameter is

- `'list'`, then returns a `polyMatrix` with the given diagonal and zero off-diagonal entries.
- `'polyMatrix'`, then extracts the diagonal.

Note. In the first case the elements of the list must be polynomial class objects. In the second case the result is a `list` or `polyMatrix` class object determined by the value of the `type` parameter.

## Value

The returned value is a

<code>list</code>	class object, when it extracts the diagonal from a <code>polyMatrix</code> , and the value of type isn't <code>'polyMatrix'</code> .
<code>polyMatrix</code>	class object, when builds a matrix from the given diagonal or when returns the diagonal of a <code>polyMatrix</code> , and the <code>type="polyMatrix"</code> .

## See Also

[polyMatrix-package](#).

## Examples

```
# ---
# case of real matrices

m<-matrix(1:12,3,4)
m
diag(m) # first type usage

v<-c(1,5,9) # second type usage
diag(v)
diag(v,4)
diag(v,4,2)
diag(v,ncol=4)

# ---
# case of polynomial matrices

# first kind usage: catch the diagonal elements

px<-polyMgen.d(3,3,rawData=ch2pn(
  c("-3 + z^2", "2 + 4*z", "-z^2",
    "1", "2", "3 + z",
    "2*z", "0", "2 - 3*z"), "z"), byrow=TRUE)
class(px) # "polyMdlist" "polyMatrix"
px

w<-diag(px) # the default: type="list"
```

```

class(w) # "list"
# List of 3
# $ :Class 'polynomial' num [1:3] -3 0 1
# $ :Class 'polynomial' num 2
# $ :Class 'polynomial' num [1:2] 2 -3
w

w<-diag(px,type="polyMatrix")
class(w) # "polyMdlst" "polyMatrix"
w

# second kind usage: compose a diagonal polyMatrix

ci<-c(4,1,3,2)
v<-vector("list",length(ci))
for(i in 1:length(ci))
  v[[i]]<-polynom::polynomial(c(rep(0,ci[i]),1))
class(v) # "list"
v

diag(v)
diag(v,4)
diag(v,3)
diag(v,5)
diag(v,3,5)

pd<-diag(v,4,5)
class(pd) # "polyMdlst" "polyMatrix"
pd

# clean up
# rm(ci, i, m, pd, px, v, w)

```

---

dim.polyMatrix

*The dimension of a polynomial matrix*


---

### Description

Retuns the value of the \$dim element of the given polyMatrix object. Does not check the validity of the \$dim element.

### Usage

```
## S3 method for class 'polyMatrix'
dim(x)
```

### Arguments

x a 'polyMatrix' class object

**Value**

A 2 element vector which contains the dimension parameters

**Examples**

```
dim(matrix(1:12,3,4)) # dim of a real matrix

A <- polyMgen.a()
class(A)# polyMarray
dim(A) # dim of a polyMatrix
```

---

is.polyMatrix	<i>Is an object of type 'polyMatrix'?</i>
---------------	-------------------------------------------

---

**Description**

Checks whether the given object is a polyMatrix object or not.

**Usage**

```
is.polyMatrix(x)
```

**Arguments**

x                    an R object.

**Details**

is.polyMatrix returns TRUE if its argument is a polyMatrix (that is, has "polyMatrix" amongst its classes and one of the four sub-classes: "polyMarray", "polyMbroad", "polyMcells", "polyMdlist") and FALSE otherwise.

**See Also**

[pMstr](#)

**Examples**

```
pm <- polyMgen.a(2,3,5)

is.polyMatrix(polyMconvert(pm,"polyMarray"))
is.polyMatrix(polyMconvert(pm,"polyMdlist"))
is.polyMatrix(polyMconvert(pm,"polyMbroad"))
is.polyMatrix(polyMconvert(pm,"polyMdlist"))

# clean up
# rm(pm)
```

---

lead *The leading coefficient of a polynom or polynomial matrix*

---

### Description

Returns the leading coefficients of the input polynom or polynomial matrix.

### Usage

```
lead(p,method=c("matrix","column","row","element"))
```

### Arguments

**p** a [polynomial](#) or [polyMatrix-package](#) class object  
**method** controls the interpretation of the word: "leading", see the details

### Details

The four possible interpretation of the lead for a polynomial matrix are:

- **matrix**: the highest matrix coefficient of the polynomial matrix.
- **column**: taken the polynomial matrix column-wise, the row vector of the highest coefficient of each column.
- **row**: taken the polynomial matrix row-wise, the column vector of the highest coefficient of each row.
- **element**: a matrix formed by the highest coefficients of the polynomial elements of the polynomial matrix.

### Value

Returns a matrix by the same size as the polynomial matrix.

### See Also

[coefs](#), [degree](#), [const](#)

### Examples

```
lead(polynom::polynomial(0:12))
pm <- polyMgen.a()
pa <- polyMconvert(pm,"polyMarray")
pb <- polyMconvert(pm,"polyMbroad")
pc <- polyMconvert(pm,"polyMcells")
pd <- polyMconvert(pm,"polyMdlist")
lead(pa)
lead(pb)
lead(pc)
lead(pd)
```

```
rawAdat <- ch2pn(c("-3 + x^2", "2 + 4*x", "-x^2", "1", "2", "3 + x", "2*x", "0", "2 - 3*x" ))
px <- polyMgen.d(3,3,rawData=rawAdat)

# clean up
# rm(rawAdat)

px

lead(px)
lead(px,method="matrix")
lead(px,method="row")
lead(px,method="column")
lead(px,method="element")

# clean up
# rm(pm, pa, pb, pc, pd, px)
```

---

matrixMinMax

*Maximums and minimums for numeric matrices*

---

## Description

Calculate the maximums or minimums column-wise or row-wise, depending on the called method.

## Usage

```
colMax(matrix) # column maximums
colMin(matrix) # column minimums
rowMax(matrix) # row maximums
rowMin(matrix) # row minimums
```

## Arguments

matrix            a matrix class object

## Value

A vector by the column or row maximums or minimums of the given matrix.

## See Also

[colMin](#), [rowMax](#), [rowMin](#)

**Examples**

```

set.seed(123)
M <- matrix(rpois(12,3),3,4)
M
# 2 5 3 3
# 4 6 5 6
# 2 0 3 3

colMax(M) # c(4,6,5,6)
colMin(M) # c(2,0,3,3)
rowMax(M) # c(5,6,3)
rowMin(M) # c(2,4,0)
# clean up
# rm(M)

```

---

MTS2pM

---

*Converts MTS representation of a VARMA process to a polyMatrix representation*


---

**Description**

The MTS representation of VARMA process is a list of 13 elements. The necessary elements to represent a VARMA model are the c(2, 3, 4, 5, 8, 11, 12, 13) elements: ARorder, MAorder, cnst, coef, Sigma, Phi, Theta, Ph0. The other five are redundant parameters.

**Usage**

```
MTS2pM(M)
```

**Arguments**

M                    an arbitrary VARMA model list-object of the MTS package

**Details**

MTS (Multivariate Time Series) is a general package for analyzing multivariate linear time series, written by Ruey S. Tsay.

**Value**

An pMvarma class object, equivalent with the M input object, created by the package MTS.

**See Also**

[print.pMvarma](#), [print.polyMatrix](#)

**Examples**

```

# runs longly
library(MTS)
set.seed(1)
yt <- VARMAsim(300, arlags=1, malags=1,
              phi=matrix(c(0.2, -0.6, 0.3, 1.1), 2, 2),
              theta=matrix(c(-0.5, 0, 0, -0.5), 2, 2),
              sigma=diag(2))$series
M <- VARMA(yt, p=2, q=2, include.mean=TRUE)
M[-c(1, 6, 7, 9, 10)]
pMvarma <- MTS2pM(M)
print(pMvarma, style="broad", digits=3)
pMvarma
print(pMvarma, "matrix", digits=3)

# clean up
# rm(yt, M, pMvarma)

```

Ops.polyMatrix

*Arithmetic Ops Group Methods for polyMatrix class objects***Description**

Allows arithmetic operations by left hand side polynomial matrices. Contains operators such as addition, multiplication, division, etc.

**Usage**

```

## S3 method for class 'polyMatrix'
Ops(e1, e2)

```

**Arguments**

e1                    an object of class polyMatrix  
e2                    an object of class numeric, character or polyMatrix

**Value**

A c("polyMdlist", "polyMatrix") class polynomial matrix which is the result obtained by performing the operation on the two arguments.

**Author(s)**

Prohle Tamas

**See Also**

[polyMatrix-package](#), [Ops](#)

**Examples**

```
X <- polyMgen.d(2,2, rawData=ch2pn(c("1","1+x^2","x","0")))
Y <- polyMgen.d(2,2, rawData=ch2pn(c("2","2*x+x^2","x","-1")))

X # signing a polyMatrix
-X
+X

X+1 # polyMatrix + numeric
X-1

1+X # numeric + polyMatrix
1-X

(1-X)*2 # polyMatrix * numeric
(-2)*(1-X)

X # polyMatrix + matrix
diag(2)+X+diag(2)
-diag(2)-X-diag(2)

X-M2pM(diag(2)) # polyMatrix - polyMatrix -- OK
X+Y
X-Y

# polyMatrix * polynom -- three solutions:
X*"1+3*x+2*x^2" # as a string
"1+3*x+2*x^2"*X

X*diag(list(ch2pn("1+3*x+2*x^2")),dim(X)[2]) # as a diagonal polyMatrix
diag(list(ch2pn("1+3*x+2*x^2")),dim(X)[2])*X

# X*polynom::polynomial(c(1,3,2)) # as a polynomial
# polynom::polynomial(c(1,3,2))*X # does not works!

# polyMatrix product
Z<-X*Y
Z
const(X)
const(Y)
const(X)%*%const(Y) # conventional multiplication of two matrices
const(Z) # similar: the constant of the product polyMatrix
const(X)*const(Y) # dissimilar: element wise product of two conventional matrices

# polyMatrix power
X
```



```

X^0
X^1
X^2
X*X
X^3

# clean up
# rm(X, Y, Z)

```

---

pMadj

*The adjugate of the given polynomial matrix*


---

### Description

The adjugate of the given matrix. Also the transpose of the matrix formed from the determinants of submatrices multiplied by the chessboard rule signs.

### Usage

```
pMadj(pm)
```

### Arguments

```
pm          a 'polyMatrix' class object
```

### Value

A polyMatrix class object, the adjugate of the given polynomial matrix.

### See Also

[pMdet](#), [pMsub](#)

### Examples

```

(A<-polyMgen.a(2,2))
# 1 + 2*x + 3*x^2          7 + 8*x + 9*x^2 + 10*x^3
# 4 + 5*x + 6*x^2          11 + 12*x
pMdet(A)
# -17 - 33*x - 61*x^2 - 97*x^3 - 104*x^4 - 60*x^5
pMsub(A,1,1)*pMsub(A,2,2)-pMsub(A,1,2)*pMsub(A,2,1)
# -17 - 33*x - 61*x^2 - 97*x^3 - 104*x^4 - 60*x^5
(B<-pMadj(A))
# 11 + 12*x                -7 - 8*x - 9*x^2 - 10*x^3
# -4 - 5*x - 6*x^2         1 + 2*x + 3*x^2
A*B          # diagonal
pMdet(A)

B*A
pMdet(A)

```

```

# real matrices

X<-matrix(c(3,0:7), ncol = 3)
X
# 3 2 5
# 0 3 6
# 1 4 7

det(X) # -12
solve(X)*det(X)
# -3 6 -3
# 6 16 -18
# -3 -10 9
pMadj(M2pM(X)) # the same

# clean up
# rm(A, B, X)

```

---

pMbas

*Bastion elements of a polynomial matrix*


---

## Description

Elements of a matrix or polyMatrix object, from non-beating positions for bastion in the matrix as a chess board.

## Usage

```
pMbas(pm, ki, byrow)
```

## Arguments

pm	a polynomial matrix object
ki	a permutation of the column numbers
byrow	logical. If FALSE (the default) the elements of ki are column indexes, if TRUE these are row indexes.

## Details

Usual

## Value

A list of polynomial class bastion elements of the given polyMatrix determined by the given permutation ki. in a pVector object

**See Also**[pMdet](#)**Examples**

```

A<-polyMgen.a()
class(A)# "polyMarray" "polyMatrix"
dim(A)# 2 x 3
A
pMbas(A,c(2,3),byrow=TRUE) # the [1,2] and [2,3] elements
pMbas(A,c(2,2,1),byrow=FALSE) # the [2,1], [2,2] and [1,3] elements
pMbas(A,c(2,2),byrow=FALSE) # the [2,1] and [2,2] elements
# pMbas(A,c(2,2,1),byrow=TRUE) # Error: Index vector too long!

A<-polyMgen.d(3,3,
  rawData=ch2pn(c("1","0","-1",
                 "2","1","-1",
                 "0","1","1")),byrow=TRUE)
A
pMbas(A,c(2,3,1),byrow=TRUE) # the [1,2], [2,3] and [3,1] elements
pMbas(A,c(2,3,1),byrow=FALSE) # the [2,1], [3,2] and [1,3] elements

# clean up
# rm(A)

```

---

pMcol

*A column of the given polyMatrix*

---

**Description**

Picks up a given column of the given matrix

**Usage**

```
pMcol(pm, which = 1)
```

**Arguments**

pm	a polyMatrix class object
which	the serial number of the required column

**Value**

A pVector class list of the elements of the column 'which' of the polynomial matrix 'pm'.

**See Also**[pMrow](#)

**Examples**

```
A <- polyMgen.a()
A

pMcol(A,2)

# clean up
# rm(A)
```

---

pMdet

---

*Calculate the determinant of a real or polynomial matrix*


---

**Description**

The determinant of the given square matrix.

**Usage**

```
pMdet(pm)
```

**Arguments**

```
pm          a polyMatrix class object
```

**Value**

A numeric or polynomial class polynom.

**See Also**

[pMsub](#), [pMadj](#)

**Examples**

```
rd <- c(3,0:7)

D <- polyMgen.a(3,3,rawData=rd,degree=1,symb="x")
D
# 3          5 + 6*x  2 + 3*x
# 1 + 2*x    7 + 3*x  4 + 5*x
# 3 + 4*x    x        6 + 7*x

pMdet(D) # 114 + 150*x + 22*x^2 + 6*x^3

elem <- function(x,k,j) (pMbas(x,c(rep(1,k-1),j),byrow=TRUE)$dlist[[k]])[[1]]
d11 <- elem(D,1,1);d12 <- elem(D,1,2);d13 <- elem(D,1,3)
d21 <- elem(D,2,1);d22 <- elem(D,2,2);d23 <- elem(D,2,3)
d31 <- elem(D,3,1);d32 <- elem(D,3,2);d33 <- elem(D,3,3)
```

```

polyMgen.d(3, 3, rawData=list(d11,d12,d13,d21,d22,d23,d31,d32,d33), symb="x", byrow=TRUE)

# direct det calculation
d11*d22*d33+d12*d23*d31+d13*d21*d32-(d13*d22*d31+d11*d23*d32+d12*d21*d33)
# 114 + 150*x + 22*x^2 + 6*x^3

D <- polyMgen.a(3,3,rawData=rd,degree=0)
D

M <- matrix(rd, ncol = 3)
M

c(pMdet(D),det(M)) # det of a polyMatrix == det of a real matrix (!)

# clean up
# rm(D, d11, d12, d13, d21, d22, d23, d31, d32, d33, elem, M, rd)

```

---

pMdiag

*Generates a diagonal polynomial square matrix*


---

## Description

The generated matrix a diagonal matrix of the given dimension with the diagonal elements given as input.

## Usage

```
pMdiag(p, diag_dim, symb="x")
```

## Arguments

p	a polynomial object or list of polynomial objects for diagonal elements
diag_dim	the row and column size of the diagonal matrix
symb	the symbol used in the polynomial matrix

## Value

A 'polyMatrix' class type polynomial matrix with given diagonal elements.

## See Also

[diag](#)

**Examples**

```
pMdiag(ch2pn("1"),3)
pMdiag(ch2pn("1+2*x+3*x^2"),3)
pMdiag(ch2pn(c("x","2*x","3*x","4*x")),3)
pMdiag(ch2pn(c("x","2*x","3*x","4*x")),6)
```

---

pMkmm

*The Kronecker indices of a polynomial matrix*

---

**Description**

Calculates the Kronecker indices of a polynomial matrix.

**Usage**

```
pMkmm(pm)
```

**Arguments**

pm                    a polynomial matrix

**Value**

A vector of the Kronecker indices.

**Note**

The method doesn't work yet.

**See Also**

[polyMatrix-package](#)

**Examples**

```
polyMgen.a()
#% end of donttest
```

---

pMprod	<i>Product of the elements of the given polynomial vector</i>
--------	---------------------------------------------------------------

---

**Description**

The product of the elements of the vector pm given in polyMatrix class object format.

**Usage**

```
pMprod(pm)
```

**Arguments**

pm                    a polyMatrix class object

**Details**

The input must be a polyMatrix class vector object. The result is a polynomial class polynom.

**Value**

A polynomial which is the product of the elements of the argument 'pm'.

**See Also**

[pVsk](#)

**Examples**

```
set.seed(32)
A <- polyMgen.a(1,2)
A
pMprod(A)

# clean up
# rm(A)
```

pMrow *A row of the given polyMatrix*

---

**Description**

Picks up a given row of the given polyMatrix.

**Usage**

```
pMrow(pm, which = 1)
```

**Arguments**

pm                    a polyMatrix class object  
which                the serial number of the required column

**Value**

A pVector class list of the elements of the which row of the pm polynomial matrix.

**See Also**

[pMrow](#)

**Examples**

```
A <- polyMgen.a()
A
pMrow(A, 2)

# clean up
# rm(A)
```

---

pMsgn *Change the sign of a polynomial matrix object*

---

**Description**

Multiplies the given polyMatrix by -1, and returns the -1 times the given polynomial matrix.

**Usage**

```
pMsgn(pm)
```

**Arguments**

pm                    a polynomial matrix object



**Value**

The polynomial matrix for which the  $\text{pm} + \text{pMsgn}(\text{pm})$  equals a zero polynomial matrix.

**See Also**

[Ops.polyMatrix](#)

**Examples**

```
A <- polyMgen.a()
A
class(A) # "polyMarray" "polyMatrix"

A - polyMconvert(A,"polyMbroad")
A - polyMconvert(A,"polyMcells")
A - polyMconvert(A,"polyMdlist")

A + pMsgn(polyMconvert(A,"polyMbroad"))
A + pMsgn(polyMconvert(A,"polyMcells"))
A + pMsgn(polyMconvert(A,"polyMdlist"))

# clean up
# rm(A)
```

---

pMstr

*polyMatrix object consistency check*

---

**Description**

Checks the consistency of a polyMatrix object. In the polyMatrix there are four different but equivalent storing methods of polynomial matrices.

**Usage**

```
pMstr(pm)
```

**Arguments**

pm                    a polynomial matrix

**Value**

A logical value of the consistency of the given polynomial object. In case of inconsistency an information about the errors.

**See Also**

[polyMgen.a](#), [polyMgen.b](#), [polyMgen.c](#), [polyMgen.d](#)

**Examples**

```

A <- polyMgen.a(2,3,5)
B <- polyMconvert(A,"polyMdlst")

# pMstr(B)$cns

## class of elements: polynomial
# B[[1]][[1]]<-1
# str(B)
# (pMstr(B))

## class of sublists: list
# B[[1]]<-1:length(B[[1]])
# str(B)
# pMstr(B)

# absence of an element
# B[[1]]<-as.list(B[[1]][-1])
# str(B)
# pMstr(B)[[3]]

# clean up
# rm(A, B)

# % end of donttest

```

---

pMsub

*A submatrix of a polynomial matrix*


---

**Description**

Retains or deletes the *i*-th rows and the *j*-th column, depending of the sign of these indices.

**Usage**

```
pMsub(pm, i, j)
```

**Arguments**

pm	a polynomial matrix
i	the number of rows to retain or delete
j	the number of columns to retain or delete

**Details**

If the row or column number is NULL, that means all elements from the given columns or rows respectively. If *j* is not given, that means a symmetric submatrix.

**Value**

A polynomial matrix which is a submatrix of the given matrix in 'polyMdlist' format.

**See Also**

[pMdet](#), [pMadj](#)

**Examples**

```
A <- polyMgen.a(3,4,1:24,degree=1)
A
pMsub(A, 2, 3)
pMsub(A, 1,NULL)
pMsub(A, NULL, 3)
pMsub(A, 1:2, 2:4)
pMsub(A, -3, 2:5)
pMsub(A, 1:2)

# clean up
# rm(A)
```

---

pn2ch

*Converts a polynom class object to a character class object*

---

**Description**

Takes a polynom class object and returns a character class object looks like the print image of the polynom object.

**Usage**

```
pn2ch(x, symb = "x", digits = getOption("digits"), decreasing = FALSE, ...)
```

**Arguments**

x	the given polynom class object
symb	the symbol of polynom
digits	the number of significant digits to be printed
decreasing	the desired order of the terms of the polynomial
...	additional arguments

**Details**

A technical subrutin to convert a polynom object to a character object.

**Value**

A character class object.

**See Also**[pprt](#)**Examples**

```

p <- polynom::polynomial(0:12)
pn2ch(p)

p <- polynom::polynomial(12:0)
pn2ch(p)

# clean up
# rm(p)

```

---

**polyMconvert***Conversion between the pairs of the four polyMatrix subclasses*

---

**Description**

The `polyMatrix` package has 4 different but equivalent methods to store the polynomial matrices.

This function provides a conversion between the 4 methods. In the background operates one of the existing 12 subrutines, corresponding to the sub-class of the given input object and the required sub-class of the output object.

**Usage**

```
polyMconvert(pm, newclass)
```

**Arguments**

<code>pm</code>	an arbitrary <code>polyMatrix</code> class object
<code>newclass</code>	a class identifier character string, one of the following: <code>"polyMarray"</code> , <code>"polyMbroad"</code> , <code>"polyMcells"</code> or <code>"polyMdlist"</code>

**Value**

A `polyMatrix` class object, equivalent with the `pm` input object, but stored in the new, given format by the `newclass` parameter.

**See Also**[polyMatrix-package](#)

**Examples**

```

set.seed(2)
pa <- polyMgen.a(rand=function(x) rpois(x,1)) # Poisson(1) distributed coefficients
class(pa) # "polyMarray" "polyMatrix"
str(pa)
pa

pb <- polyMconvert(pa,'polyMbroad')
class(pb) # "polyMbroad" "polyMatrix"
str(pb)
pb

pc <- polyMconvert(pa,'polyMcells')
class(pc) # "polyMcells" "polyMatrix"
str(pc)
pc

pd <- polyMconvert(pa,'polyMcells')
class(pd) # "polyMdlist" "polyMatrix"
str(pd)
pd

px <- polyMconvert(pa,'polyMarray')
class(px) # "polyMarray" "polyMatrix"
str(px)
px

# clean up
# rm(pa, pb, pc, pd, px)

```

---

polyMgen

---

*Generate a polyMatrix class polynomial matrix*


---

**Description**

A complex tool to generate a polynomial matrix in ‘polyMatrix’ form. The ‘polyMatrix’ object contains the following three invariant elements: the \$dim, \$degree and \$symb independently of the sub-class of the object. The \$dim is the size of the matrix. The \$degree is a matrix of non-negative numbers, the degree of the polynomial elements of the polynomial matrix. The \$symb the symbol to print and identify the reference to the algebraic set over which the polynom defined – sorry, this option not fully works.

**Usage**

```
polyMgen(nrow, ncol, rawData, symb, rand, degree, byrow, sm="polyMarray", ...)
```

**Arguments**

nrow	the desired number of rows
ncol	the desired number of columns
degree	the desired degrees of polynomials when it is filled randomly
rowData	the data to fill with the polynomial matrix. In case of polyMgen.a, polyMgen.b and polyMgen.c a vector of the required coefficients of the polynomials. The case of polyMgen.d is different: here the rowData is a list of <a href="#">polynomial</a> class objects
symb	the desired polynom symbol
rand	the name of the random generator used to generate the coefficients of a random polynomial matrix
byrow	logical. If FALSE (the default) the matrix is filled by columns, if TRUE the matrix is filled by rows
sm	storage method: polyMarray (the default) or \ polyMbroad, polyMcells, polyMdlist
...	additional arguments

**Details**

The four possible methods to generate the polynomial matrix from the given material rowData or (the default) or random values:

- ‘array’, when the coefficient matrices of the polinomial matrix are stored in two independent element of the list of the polyMatrix: the constant matrix in \$const, and the coefficients of the first, second... degree of the polynomial in the first, second,... element of the \$array. In this case the sub-class of the generated polyMatrix object is polyMarray.
- ‘broad-matrix’, when the coefficients are stored in one broad matrix in the \$broad element of the polyMatrix object. The size of this broad matrix is: nrow x (ncol\*(d+1)), when the degree of the nrow x ncol size polynomial matrix is d. In this case the sub-class of the generated polyMatrix object is polyMbroad.
- ‘list of cells’, when the nrow x ncol size coefficient matrices are stored in d+1 element of the \$cells list element of the polyMatrix object. In this case the sub-class of the generated polyMatrix object is polyMcells.
- ‘double list’, when the elements of the polynomial matrix are stored in the form of polynomial class objects in a nrow x ncol element double list. In this case the sub-class of the generated polyMatrix object is polyMdlist.

**Value**

A polyMatrix class object with a sub-class polyMarray, polyMbroad, polyMcells or polyMdlist.

**See Also**

[polyMatrix-package](#), [polyMgen.a](#), [polyMgen.b](#), [polyMgen.c](#), [polyMgen.d](#)

**Examples**

```

polyMgen.a() # default size & coefficients & rank

polyMgen.a(2,3,1:6) # given coefficients & default rank
polyMgen.a(2,3,1:6,degree=1) # given coefficients & rank
polyMgen.a(2,3,1:36,degree=matrix(0:5,2,3)) # given coefficients & ranks
polyMgen.a(2,3,1:12,degree=matrix(2:0,2,3)) # given coefficients & ranks

polyMgen.a(rand=TRUE) # normally distributed coefficients

polyMgen.a(rand=rexp) # exponentially distributed coefficients

pois.vg.fv <- function(x) rpois(x,1)
polyMgen.a(rand=pois.vg.fv) # Poisson(1) distributed coefficients
rm(pois.vg.fv)

polyMgen.b() # class="polyMbroad", broad matrix form
polyMgen.c() # class="polyMcells", list of coefficient matrices
polyMgen.d() # class="polyMdlist", dubble list

polyMgen.d(2,2,
  rawData=list(polynom::polynomial(1),
               polynom::polynomial(c(0,0,1)),
               polynom::polynomial(c(0,1)),
               polynom::polynomial(0)))

px <- polyMgen.d(3,3,rawData=ch2pn(
  c("-3 + z^2","2 + 4*z","-z^2",
    "1","2","3 + z",
    "2*z","0","2 - 3*z"),"z"))
class(px) # "polyMdlist" "polyMatrix"
px

px <- polyMgen.d(3,3,rawData=ch2pn(
  c("-3 + z^2","2 + 4*z","-z^2",
    "1","2","3 + z",
    "2*z","0","2 - 3*z"),"z"),byrow=TRUE)
class(px) # "polyMdlist" "polyMatrix"
px

polyMgen.d()
polyMgen.d(rand=TRUE)
polyMgen.d(rand=TRUE,degree=2)
polyMgen.d(degree=3)
polyMgen.d(degree=NULL)

# clean up
# rm(px)

```

---

polyMul

*Multiplication of two polynomial by matrix multiplication*

---

**Description**

...

**Usage**

polyMul(p, q)

**Arguments**

p                   ... polyMgen

q                   ... polyMgen

**Details**

more details than the description above

**Value**

Describe the value returned!! If it is a LIST, use

comp1               Description of 'comp1'

**Note**

further notes

**Author(s)**

who you are

**References**

references to the literature

**See Also**

objects to See Also as [polyMatrix-package](#)



**Examples**

```

set.seed(12345)
p <- polynom::polynomial(rpois(rgeom(1, .2)+1,2))
q <- polynom::polynomial(rpois(rgeom(1, .2)+1,2))
p
q
p * q
as.numeric(p * q) # 9 30 30 18 19 14 7 3
polyMul(p, q)
polyMul(q, p)

# clean up
# rm(p, q)

```

pprt

*Intelligent print of a polynom object***Description**

Calls the pn2ch converter, and prints the polynomial considering shift parameter and the width of the actual consol window.

**Usage**

```
pprt(x, symb = "x", shift = 0, digits = getOption("digits"), decreasing = FALSE, ...)
```

**Arguments**

x	the polynom object to be printed
symb	the symbol used in the print
shift	the beginnig shift
digits	the width of the coefficients to be printed
decreasing	indicator of the order of powers terms: decreasing or not
...	additional arguments

**See Also**

[pn2ch](#)

**Examples**

```

p <- polynom::polynomial(0:12)
pprt(p)
pprt(p, sh=3)
pprt(p, sh=3, symb="L")
# clean up
# rm(p)

```

---

predict.charpn	<i>Calculate the value of a characteristic polynomial for a polyMatrix argument</i>
----------------	-------------------------------------------------------------------------------------

---

### Description

The 'polynom::predict.polynomial()' method works by real coefficients only but it works for real or complex and matrix argument also. But in the case of matrix argument uses the elementwise product. The 'polyMatrix::predict' method evaluate the polynom by the usual matrix product definition.

### Usage

```
## S3 method for class 'charpn'
predict(object,pM,...)
```

### Arguments

object	a 'charpn' class object
pM	a 'polyMatrix' class object
...	additional arguments

### Value

value	A 'polynomial' class object
-------	-----------------------------

### See Also

[predict.polynomial](#), [predict.polyMatrix](#)

### Examples

```
pm <- polyMgen.d(2,2,rawData=ch2pn(c("1", "x^2", "x", "0")))
pm # 1, z^2\ z, 0

predict(pm,2) # matrix(c(1,4,2,0),2)

# predict the result of a linear model
x <- 1:5;y <- rnorm(5);predict(lm(y~x)) # the used method: predict.lm()

# clean up
# rm(pm, x, y)
```

---

predict.polyMatrix      *Calculate the value of a polynomial matrix for real or complex values*

---

### Description

Calculate the value of the polynom elements of the 'polyMatrix' class object for real and complex argument also.

### Usage

```
## S3 method for class 'polyMatrix'
predict(object,M,...)
```

### Arguments

object	a 'polyMatrix' class object
M	a real or complex argument
...	additional arguments

### Value

A matrix the just the same size as the input, filled by the values of the polynom elements, at the given argument.

### See Also

[predict.polynomial](#), [predict.charpn](#)

### Examples

```
# for predict the value of a polynomial matrix at a real or complex value
#   the used method: predict.polyMatrix()

pm <- polyMgen.d(2,2,ch2pn(c("1","x","x^2","0")))
pm # 1, x^2 \ x, 0

predict(pm,2) # 1, 4 \ 2, 0

# for predict the result of a linear model
#   the used method: predict.lm()

x<-1:5;y<-rnorm(5);predict(lm(y~x))

# clean up
# rm(pm, x, y)
```

---

predict.polynomial      *Calculate the value of a 'polynomial' for real, complex and matrix argument*

---

### Description

The 'polynom::predict.polynomial()' method works for real, complex and matrix argument also. But in the case of matrix argument it uses the elementwise calculations instead the matrix multiplication. The 'polyMatrix::predict.polynomial()' calculate the result by the usual matrix product definition except the case, when the parameter meth equals by "as.in.the.polynom.package".

### Usage

```
## S3 method for class 'polynomial'
predict(object,M, meth=c("as.matrix", "as.in.the.polynom.package"), ...)
```

### Arguments

object	a numeric, matrix or polyMatrix class object
M	a polynomial class object
meth	If the value of this parameter as the default, "as.matrix" then calculate by matrix multiplications. Otherwise it calculate by elementwise multiplications.
...	additional arguments

### Value

The is a numeric, numeric, matrix or polyMatrix class object depending on the class of the input

### See Also

[predict.polyMatrix](#), [predict.charpn](#)

### Examples

```
p <- polynom::polynomial(1:3)
p # 1 + 2*x + 3*x^2

# predict a polynom for real values
predict(p,1) # 6

# predict a polynom for complex values
predict(p,1i) # -2+2i

# predict a polynom for matrices
M <- matrix(c(1,-1),2,2);
M
predict(p,M) # 3,2 \ -2, -1
```

```

# mimiking the elementwise calculation of the masked "polynom::predict" method
predict(p,M,meth="as.in.") # 6, 6 \ 2, 2

# predict a polynom for a polynomial matrix
pM <- polyMgen.d(2,2, rawData=ch2pn(c("1","x^2","x","0")))
pM # 1, x \ x^2, 0
predict(p,pM) # method: predict.polyMatrix()
# 6 + 3*z^3 5*z
# 5*z^2      1 + 3*z^3

# ---
# predict the result of a linear model
x <- c(1,3,4,1,0);
y <- c(27,81,54,27,18)
predict(lm(y~x)) # method: predict.lm()
# 31 57 70 31 18

# clean up
# rm(p, M, pM, x, y)

```

---

print

*Prints a polynomial matrix or a varma model in the given form*


---

## Description

Printing method for class `polyMatrix` and `pMvarma`.

## Usage

```

## S3 method for class 'polyMatrix'
print(
  x, style=c("matrix", "polynom", "broad", "raw"),
  round=NULL,digits=getOption("digits"), shift = 3, decreasing = FALSE, ...
)
## S3 method for class 'pMvarma'
print(
  x, style=c("matrix", "polynom", "broad", "raw"),
  round=NULL,digits=getOption("digits"), shift = 3, ...
)

```

## Arguments

<code>x</code>	a <code>polyMatrix</code> or <code>pMvarma</code> class object to be printed
<code>style</code>	one of the four printing types
<code>round</code>	rounds as the <code>base::round()</code> function
<code>digits</code>	the number of significant digits to be printed
<code>shift</code>	the beginnig shift
<code>decreasing</code>	the terms of the polynomial in decreasing order or not
<code>...</code>	additional arguments

**See Also**[print](#)**Examples**

```

set.seed(1)
pm <- polyMgen.a(rand=function(x) rpois(x,1))

pa <- polyMconvert(pm,"polyMarray") # class: "polyMarray" "polyMatrix"
pb <- polyMconvert(pm,"polyMbroad") # class: "polyMbroad" "polyMatrix"
pc <- polyMconvert(pm,"polyMcells") # class: "polyMcells" "polyMatrix"
pd <- polyMconvert(pm,"polyMdlist") # class: "polyMdlist" "polyMatrix"
# clean up
# rm(pm)

# the default, the "matrix" print image style: matrix of polynomials
pa
pb
pc
pd

# the three other print image style:
print(pa,"poly")
print(pa,"broad")
print(pa,"raw")

print(pb,"poly")
print(pb,"broad")
print(pb,"raw")

print(pc,"poly")
print(pc,"broad")
print(pc,"raw")

print(pd,"poly")
print(pd,"broad")
print(pd,"raw")

# clean up
# rm(pa,pb,pc,pd)

varma <- polyMgen.varma()

varma
print(varma,"matrix") # the same print image
print(varma,"poly")
print(varma,"broad")
print(varma,"raw")

# clean up
# rm(varma)

```

---

 proper

*The polynomial matrix is column//row proper or not*


---

### Description

The program returns a logical value, whether the given polynomial matrix is column or row proper or both. A ‘proper’ matrix called in other way column or row ‘reduced’.

### Usage

```
proper(pm,type=c("col","row","both"),print=c(TRUE,FALSE))
```

### Arguments

pm	a polyMatrix class polynomial matrix
type	the type of rating row//col//both
print	the kind of printing

### Details

The program calculates first the column or row associated matrices, and the answer depends on there ranks. A polynomial matrix is ‘proper’ if the associated matrix has a full rank. The program has an invisible silent output.

### Value

Logical: TRUE or FALSE. The associated matrix is only an optional part of the output, and the print.

### See Also

[coefs](#), [lead](#)

### Examples

```
pm <- polyMgen.d(2,2,rawData=ch2pn(c("-1+7*x","x","3-x+x^2","-1+x^2-3*x^3")))
pm
proper(pm) # the default is the col-property labeling
(proper(pm,print=FALSE)) # the invisible output, without printing
proper(pm,"col")
proper(pm,"row")
proper(pm,"both")

# clean up
# rm(pm)
```

---

pVsk

*The scalar product of two polynomial vectors*

---

### Description

If pMy is NULL, then the result is the sum of squares of the elements of pMx. Otherwise equals the scalar product of the two given polynomial vectors.

### Usage

```
pVsk(pMx, pMy=NULL)
```

### Arguments

pMx                    a polyMatrix class row or column vector

pMy                    a polyMatrix class row or column vector

### Details

The two vectors must have the same length.

### Value

A polynomial class object, which is the sum of the elementwise product of the two vectors.

### See Also

[pMprod](#)

### Examples

```
A <- polyMgen.d(2,2,rawData=ch2pn(c("-3", "2+4*z", "-z^2", "1"), "z"))
A

pMcol(A,1) # ("-3", "2 + 4*x")
pVsk(pMcol(A,1)) # "13 + 16*x + 16*x^2"

pMrow(A,2) # ("2 + 4*x", "1")
pVsk(pMcol(A,1),pMrow(A,2)) # "-4 - 8*x"

# clean up
# rm(A)
```



---

symb	<i>The printing symbol of the given polynomial matrix</i>
------	-----------------------------------------------------------

---

**Description**

Get the printing symbol of the given polynomial matrix

**Usage**

```
symb(pm)
```

**Arguments**

pm                    a polyMatrix class object

**Details**

The polynomial matrix objects contains a character to sign the variable of the polynomials. The system default is 'x'.

**Value**

One character, which used to print the polynomials in default cases

**See Also**

[dim.polyMatrix](#), [degree.polyMatrix](#), [degree.polynomial](#)

**Examples**

```
pM <- polyMgen.d(2,2,rawData=
  ch2pn(c("-3+s^3","2+4*s","s^2","1"),symb="s"))
pM

# -3 + x^3   x^2
#  2 + 4*x   1

symb(pM) # "x"

pM <- polyMgen.d(2,2,rawData=
  ch2pn(c("-3+x^3","2+4*x","x^2","1")),symb="L")
pM

# -3 + L^3   L^2
#  2 + 4*L   1

symb(pM) # "L"

# clean up
# rm(pM)
```

---

t.polyMatrix	<i>Matrix transpose of a polyMatrix class object</i>
--------------	------------------------------------------------------

---

### Description

The method first convert the storage method of the given polyMatrix object to polyMdlst class interpretation, then flips the polyMatrix over its diagonal.

### Usage

```
## S3 method for class 'polyMatrix'
t(x)
```

### Arguments

x                    polyMatrix class object

### Value

A 'polyMdlst, polyMatrix' class object, the transposed version of the given x polynomial matrix.

### See Also

The 't' in the base package.

### Examples

```
m <- matrix(1:12,3,4)
t(m) # the \code{base::t()} function

pa <- polyMgen.a()
pm <- t(pa)
dim(pm) # 3 x 2
class(pm) # "polyMdlst" "polyMatrix"
```

---

tr	<i>Trace of a 'matrix' or 'polyMatrix' class matrix</i>
----	---------------------------------------------------------

---

### Description

Returns the trace of the given matrix.

### Usage

```
tr(matrixObject)
```

**Arguments**

matrixObject a matrix or polyMatrix class object

**Details**

Calculates the sum of the diagonal elements of the given matrix.

**Value**

- a numeric class object, if the given matrix is a matrix class object
- a polynomial class object, if the given matrix is a polyMatrix class object

**See Also**

[tr.polyMatrix](#), [polyMatrix-package](#), [polynomial](#), but the [trace](#) is a debugging utility

**Examples**

```
# the case of a matrix class input object
M <- matrix(1:9,3,3)
class(M)
M
# 1  4  7
# 2  5  8
# 3  6  9
tr(M) # 15

(M <- matrix(1:12,3,4))
# 1  4  7  10
# 2  5  8  11
# 3  6  9  12
tr(M) # 15

(M <- matrix(1:12,4,3))
# 1  5  9
# 2  6  10
# 3  7  11
# 4  8  12
tr(M) # 18

# case of polyMatrix class input objects
pM <- polyMgen.d(3,3,rawData=
  ch2pn(c("-3 + z^2","2 + 4*z","-z^2",
         "1",          "2", "3 + z",
         "2*z", "0", "2 - 3*z"), "z"), byrow=TRUE, symb="z")
class(pM) # "polyMdlst" "polyMatrix"
pM

( p <- tr(pM) ) # 1 - 3*x + x^2
class(p) # "polynomial"
```

```
# clean up  
# rm(M, pM, p)
```

---

triang_Euclidean	<i>Triangularization of a polynomial matrix by Euclidean division metho</i>
------------------	-----------------------------------------------------------------------------

---

**Description**

Triangularization of a polynomial matrix by Euclidean division metho

**Usage**

```
triang_Euclidean(pm)
```

**Arguments**

pm                    matrix to triangularize

**Details**

The method use the for polynomilas extended Euclidean algorithm.

This method search a solution of the triangulrization by the method of Sylvester matrix, descripted in the article Labhalla-Lombardi-Marlin (1996).

**Value**

Upper tringular matrix 'T' and transformation matrix 'U'.

**Author(s)**

Nikolai Ryzhkov, <namezys@gmail.com>

**References**

Thomas Kailaith:Linear Systems, Prentice-Hall, 1980, pp 373-376

**See Also**

triang\_Sylvester

---

triang\_Interpolation    *Triangularization of a polynomial matrix by interpolation method*

---

### Description

The parameters ‘point\_vector’, ‘round\_digits’ can significantly affect the result.

### Usage

```
triang_Interpolation(
  pm,
  point_vector,
  round_digits = 5,
  eps = .Machine$double.eps^0.5
)
```

### Arguments

pm	source polynomial matrix
point_vector	vector of interpolation points
round_digits	we will try to round result on each step
eps	calculation zero errors

### Details

Default value of ‘eps’ usually is enough to determinate real zeros.

In a polynomial matrix the head elements are the first non-zero polynomials of columns. The sequence of row indices of this head elements form the shape of the polynomial matrix. A polynomial matrix is in left-lower triangular form, if this sequence is monoton increasing.

This method offers a solution of the triangularization by the Interpolation method, described in the article of Labhalla-Lombardi-Marlin (1996).

### Value

Transformaiton matrix

### Examples

```
A <- polyMgen.d(3,2,ch2pn(c("x-1", "2", "0", "x^2-1", "2*x+2", "3")))
```

```
triang_Interpolation(A, -2:2)
# 0.79057 - 0.31623*x + 0.15812*x^2    -0.57735 - 0.57735*x
# 0.47434 - 0.15811*x - 1e-05*x^2    0.57735
```

```
triang_Interpolation(A, -10:10)
# 0.79057 - 0.3161*x + 0.15803*x^2    0.25574 - 0.3541*x - 0.60984*x^2
# 0.47448 - 0.15807*x                -0.25574 + 0.60984*x
```

---

triang_Sylvester	<i>Triangularization of a polynomial matrix by Sylvester method</i>
------------------	---------------------------------------------------------------------

---

### Description

The function `triang_Sylvester` triangularize the given polynomial matrix.

The `u` parameter is a necessary supplementary input without default value. This parameter give the minimal degree of the searched triangularizator to solve the problem.

### Usage

```
triang_Sylvester(pm,u, eps=ZERO_EPS)
```

### Arguments

<code>pm</code>	polynomial matrix to triangularize
<code>u</code>	the minimal degree of the triangularizator multiplicator
<code>eps</code>	toleranz limit

### Details

In a polynomial matrix the head elements are the first non-zero polynomials of columns. The sequence of row indices of this head elements form the *shape* of the polynomial matrix. A polynomial matrix is in left-lower triangular form, if this sequence is monoton increasing.

This method search a solution of the triangulrization by the method of Sylvester matrix, described in the article Labhalla-Lombardi-Marlin (1996).

### Value

<code>T</code>	the left-lower triangularized version of the given polynomial matrix
<code>U</code>	the right multiplicator to triangularize the given polynomial matrix

### Author(s)

Nikolai Ryzhkov, <namezys@gmail.com>

### References

Salah Labhalla, Henri Lombardi, Roger Marlin: Algorithm de calcule de la reduction de Hermite d'une matrice a coefficients polynomiaux, Theoretical Computer Science 161 (1996) pp 69-92

### See Also

[triang\\_Euclidean](#)

---

`%X%` *Multiplication of two polyMatrix class polynomial matrices*

---

**Description**

Matrix multiplication for polyMatrix class polynomial matrices. Multiplies the two matrices only if they are conformable.

**Usage**

```
left %X% right
```

**Arguments**

<code>left</code>	a polyMatrix class object, scalar number or polynomial
<code>right</code>	a polyMatrix class object, scalar number or polynomial

**Details**

The number of columns in `left` must be equal to number of rows in `right`.

**Value**

A polyMatrix class object which is the product of the polyMatrix class `left` and `right` matrices.

**See Also**

[polyMatrix-package](#)

**Examples**

```
pm <- polyMgen.a()
pm * t(pm)

# two constante matrices
a <- matrix(1:12,3,4)
b <- matrix(1:20,4,5)
a %**% b

a <- M2pM(a)
b <- M2pM(b)
a * b
a %X% b

pM2M(a) %**% pM2M(b)

# clean up
# rm(pm, a, b)
```

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